

Hafnium (Hf)

REFERENCE STATE

0 to 2054 K crystal, alpha
 2054 to 2500 K crystal, beta
 2500 to 4963.793 K liquid
 4963.793 to 6000 K Ideal Monatomic Gas

Refer to the individual tables for details.

$A_r = 178.49$ Hafnium (Hf)

Hf₁(ref)

T/K	C _p ^o	Enthalpy Reference Temperature = T _r = 298.15 K		Standard State Pressure = p ^o = 0.1 MPa		log K _t
		S ^o - [G ^o - H ^o (T)]/T	H ^o - H ^o (T _r)	ΔH ^o	ΔG ^o	
0	0	INFINITE	0	0	0	0
100	20.580	17.753	-65.394	-5.842	0	0
200	24.418	33.561	-43.871	-4.764	0	0
298.15	25.687	43.560	0	-2.462	0	0
300	25.708	43.560	0	0	0	0
400	26.751	51.261	44.581	0.048	0	0
500	27.692	57.332	46.543	2.672	0	0
600	28.583	62.460	48.780	5.394	0	0
700	29.435	66.932	51.060	8.208	0	0
800	30.288	70.919	53.298	11.110	0	0
900	31.120	74.534	55.459	14.097	0	0
1000	31.943	77.856	57.535	17.167	0	0
1100	32.759	80.938	59.524	20.320	0	0
1200	33.572	83.824	61.430	23.556	0	0
1300	34.372	86.543	63.258	26.872	0	0
1400	35.064	89.115	65.014	30.270	0	0
1500	35.765	91.558	66.703	33.741	0	0
1600	36.466	93.889	68.330	37.283	0	0
1700	37.167	96.121	69.899	40.894	0	0
1800	37.868	98.265	71.416	44.576	0	0
1900	38.569	100.331	72.884	48.328	0	0
2000	39.269	102.327	74.306	52.149	0	0
2054.000	39.648	103.378	75.057	56.041	0	0
2054.000	39.959	106.255	75.057	58.172	0	0
2100	34.384	107.011	75.749	60.080	0	ALPHA <- -> BETA TRANSITION
2200	35.307	108.632	77.207	65.652	0	0
2300	36.231	110.222	78.608	69.136	0	0
2400	37.154	111.784	79.957	72.713	0	0
2500	38.077	113.353	81.262	76.383	0	0
2500.000	38.077	113.353	81.262	80.228	0	0
2500.000	37.656	125.088	81.262	80.228	0	BETA <- -> LIQUID TRANSITION
2600	37.656	126.545	82.976	109.516	0	0
2700	37.656	127.966	84.616	113.281	0	0
2800	37.656	129.336	86.189	117.047	0	0
2900	37.656	130.657	87.699	120.813	0	0
3000	37.656	131.934	89.153	124.578	0	0
3100	37.656	133.169	90.553	128.344	0	0
3200	37.656	134.364	91.903	132.109	0	0
3300	37.656	135.523	93.208	135.875	0	0
3400	37.656	136.647	94.469	139.641	0	0
3500	37.656	137.739	95.690	143.406	0	0
3600	37.656	138.799	96.872	147.172	0	0
3700	37.656	139.831	98.020	150.937	0	0
3800	37.656	140.835	99.133	154.703	0	0
3900	37.656	141.814	100.215	158.469	0	0
4000	37.656	142.767	101.267	162.234	0	0
4100	37.656	143.697	102.291	166.000	0	0
4200	37.656	144.604	103.287	169.765	0	0
4300	37.656	145.490	104.258	173.531	0	0
4400	37.656	146.356	105.205	177.297	0	0
4500	37.656	147.202	106.129	181.062	0	0
4600	37.656	148.030	107.031	184.828	0	0
4700	37.656	148.840	107.912	188.593	0	0
4800	37.656	149.632	108.773	192.359	0	0
4900	37.656	150.409	109.615	196.125	0	0
4963.793	37.656	150.896	110.142	199.890	0	0
4963.793	37.996	263.754	110.142	202.292	0	LIQUID <- -> IDEAL GAS FUGACITY = 1 bar
5000	38.154	264.031	111.256	762.496	0	0
5200	39.044	265.544	117.161	763.875	0	0
5400	39.964	267.033	122.684	771.594	0	0
5600	40.910	268.503	127.866	779.494	0	0
5800	41.879	269.958	132.741	787.581	0	0
6000	42.870	271.394	137.339	795.859	0	0
				804.334	0	0

PREVIOUS March 1979 (1 atm)

CURRENT March 1979 (1 bar)

Hafnium (Hf)

Hf₁(ref)

Hf₁(cr)

Hafnium, Alpha (α-Hf)

A_r = 178.49

CRYSTAL(α)

Hafnium, Alpha (α-Hf)

T/K	Enthalpy Reference Temperature = T _r = 298.15 K		Standard State Pressure = p° = 0.1 MPa	
	C _p ^o	S° - (C _p ^o - HF(T _r))/T	H° - H°(T _r)	ΔG°
0	0	INFINITE	-5.842	0
100	20.580	17.753	-4.764	0
200	24.418	33.561	-2.462	0
250	25.110	39.086	-1.223	0
298.15	25.687	43.560	0	0
300	25.708	43.719	0.048	0
350	26.247	47.723	1.347	0
400	26.751	51.261	2.672	0
450	27.230	54.439	4.021	0
500	27.692	57.332	5.594	0
600	28.583	62.460	8.208	0
700	29.445	66.932	11.110	0
800	30.288	70.919	14.097	0
900	31.120	74.534	17.167	0
1000	31.943	77.856	20.370	0
1100	32.759	80.938	23.556	0
1200	33.572	83.824	26.872	0
1300	34.372	86.543	30.270	0
1400	35.064	89.115	33.741	0
1500	35.765	91.558	37.283	0
1600	36.466	93.889	40.894	0
1700	37.167	96.121	44.576	0
1800	37.868	98.265	48.328	0
1900	38.569	100.331	52.149	0
2000	39.269	102.327	56.041	0
2054.000	39.648	103.378	58.172	0
2100	39.970	104.260	60.003	0.129
2200	40.671	106.136	64.035	-0.009
2300	41.372	107.959	68.138	0.626
2400	42.073	109.734	72.310	-4.073
2500	42.774	111.466	76.552	1.042

log K_r

PREVIOUS

CURRENT, March 1979

Hafnium, Alpha (α-Hf)

Hf₁(cr)

$\Delta_f H_f^\circ(10\text{ K}) = 0\text{ kJ}\cdot\text{mol}^{-1}$
 $\Delta_f H_f^\circ(298.15\text{ K}) = 0\text{ kJ}\cdot\text{mol}^{-1}$
 $\Delta_f H_f^\circ = 5.908 \pm 0.2\text{ kJ}\cdot\text{mol}^{-1}$

Enthalpy of Formation
 Zero by definition.

Heat Capacity and Entropy
 The adopted thermal functions for α-Hf(cr) are derived from the studies of Collings and Ho,¹ Westrum,² Hawkins *et al.*³ and Cezaırlıyan and McClure.⁴ The mathematical and graphical treatment of these four studies yields a continuous and smooth heat capacity curve. Roberts⁵ surveyed the superconductive properties of the elements and reported a critical temperature of 0.128 K for α-Hf(cr). Since this temperature is so low, the effects of superconductivity on the thermal functions are not considered.

There are four studies¹⁻⁴ on the heat capacity of hafnium in the region 1–5 K. Only Wolcott⁶ reported the experimental data (56 data points). In the other three states, an equation (with two constants) was given to describe the entire set of experimental data. The second set of constants given by Betterton and Scarbrough⁷ are stated to be an average of the two studies of Kneip *et al.*¹ and the more recent study by Betterton and Scarbrough.⁸ However, the values appear suspect and may contain a typographical error. Nevertheless the maximum difference in the calculated values for S°(5 K) is 0.00024 cal K⁻¹·mol⁻¹ with the adopted value being S°(5 K) = 0.0038 cal K⁻¹·mol⁻¹. Similarly for C_p°(5 K) the maximum difference is 0.00024 cal K⁻¹·mol⁻¹, with the adopted value being C_p°(5 K) = 0.00638 cal K⁻¹·mol⁻¹.

In the region above 5 K, and below 350 K, there are four heat capacity studies.^{2,9-11} Cristescu and Sumon⁹ studies Hf from 13 to 210 K and reported 15 heat capacity values with a peak near 75 K. Burk and Darnell¹⁰ made heat capacity measurements (40–190 K) and reported that the peak is completely absent. The heat capacity measurements of Burk *et al.* (10–200 K),¹¹ and Westrum (5.82–348.55 K)¹² support this latter conclusion, i.e., no peak. The values of Burk *et al.*¹¹ after correction for the ~2% Zr in this sample, agree with the data of Westrum¹² between 10 and 40 K but deviate above 40 K, becoming ~5% higher at 100 K and decreasing to ~1% higher at 200 K. Above 350 K, there are four heat capacity studies and four enthalpy studies.

Enthalpy	Source (Year)	Data Points	T/K	Wt % Zr in Hf Sample
	Adenstedt (1952) ¹³	1	373	0.7
	Fieldhouse and Lang (1961) ¹⁴	14	534–1884	1.0
	Hawkins <i>et al.</i> (1963) ³	50	338–1346	2.8
	Golutvin and Maslennikova (1970) ¹⁵	12	551–1309	0.79
	Golutvin and Maslennikova (1970) ¹⁵	9	695–137	0.79
	Peletskii <i>et al.</i> (1971) ¹⁶	13 (smoothed)	1200–2200	0.66
	Arutyunov <i>et al.</i> (1972) ¹⁷	16 (smoothed)	1100–2050	0.65
	Cezaırlıyan and McClure (1975) ⁴	26	1500–2400	3.12
	Rumyanisev <i>et al.</i> (1979) ¹⁸	graph	1000–1900	-

The enthalpy studies show an unusually large scatter within each study as well as a lack of agreement between the studies. The heat capacity studies all have a similar temperature dependence in comparison with the adopted values. However, the studies of Arutyunov *et al.*,^{17,19} and Rumyanisev *et al.*,¹⁸ lie roughly 10% higher than the adopted values, whereas the study of Peletskii *et al.*¹⁶ lies 5–24% below. The studies by Arutyunov *et al.*,^{17,19} and Rumyanisev *et al.*¹⁸ suggest a sharp decrease in the heat capacity values within 50 K of the α-β transition temperature. The experimental results were corrected for this zirconium content.

Transition Data
 Refer to the β-crystal table for details.

Sublimation Data
 There are no sublimation studies involving α-Hf(cr). The enthalpy of sublimation is calculated as the difference between the enthalpy of formation of the ideal gas and the enthalpy of formation of α-Hf(cr).

References
¹E. W. Collins and J. C. Ho, *Phys. Rev.* **4B**, 349 (1971).
²E. F. Westrum, University of Michigan, personal communication, (1979).
³D. T. Hawkins, M. Onillon and R. L. Orr, *J. Chem. Eng. Data* **8**, 628 (1963).
⁴A. Cezaırlıyan and J. L. McClure, *J. Res. Nat. Bur. Stand.* **79A**, 431 (1975).
⁵B. W. Roberts, *J. Phys. Chem. Ref. Data* **5**, 581 (1976).
⁶N. M. Wolcott, *Phil. Mag.* **2**, 1246 (1957).

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J. Phys. Chem. Ref. Data, Monograph 9

Hf₁(cr)

Hafnium, Beta (β-Hf)

CRYSTAL (β)

Hafnium, Beta (β-Hf)

$S^\circ(298.15\text{ K}) = [61.104] \text{ J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$
 $T_m = 2054 \pm 50 \text{ K } (\alpha\text{-}\beta) \text{ J}\cdot\text{K}^{-1}$
 $T_m = 2500 \pm 20 \text{ K } (\beta\text{-}\beta) \text{ J}\cdot\text{K}^{-1}$

Enthalpy Reference Temperature = $T_r = 298.15 \text{ K}$
 $\Delta_f H^\circ(298.15 \text{ K}) = [18.686] \text{ kJ}\cdot\text{mol}^{-1}$
 $\Delta_{\alpha\beta} H^\circ = 5.908 \pm 0.2 \text{ kJ}\cdot\text{mol}^{-1}$
 $\Delta_{\beta\beta} H^\circ = [29.288 \pm 4.2] \text{ kJ}\cdot\text{mol}^{-1}$

Enthalpy of Formation

The enthalpy of formation is calculated from that of the α-crystal by addition of $\Delta_{\alpha\beta} H^\circ$ and the difference in enthalpy, $H^\circ(2054 \text{ K}) - H^\circ(298.15 \text{ K})$, between the α-crystal and β-crystal.

Heat Capacity and Entropy

The only heat capacity study for the β-crystal is that of Cezairiyand McClure.¹ Using a pulse heating technique, they studied the heat capacity of a sample containing 3.12% (wt) Zr in the range 2054 to 2400 K. These results were corrected by Cezairiyand and McClure¹ to represent pure β-Hf and are extrapolated linearly to the melting point, 2500 K, and to 298.15 K. The entropy at 298.15 is calculated in a manner similar to that for the enthalpy of formation.

Phase Data

Hafnium, at ambient pressures, exists in two crystal modifications. The low temperature form, α-Hf, is hexagonal close packed, an hcp(A3) structure isotypic with Mg. The high temperature form, β-Hf, is body centered cubic, a bcc(A2) structure isotypic with W. The wide variation in the observed transition temperature is undoubtedly due to the effects of various impurities, in particular, zirconium.

Transition Data

Cezairiyand and McClure² have summarized the reported transition temperatures for the α to β transition of hafnium. Their summary is given below. All temperatures were corrected to IPTS-68. The pure hafnium value reported by the cited author was corrected for the zirconium content of the alloy. Hulgren *et al.*,¹⁸ based on data available through 1965, recommended $T_m = 2013 \pm 20 \text{ K}$. We adopt $T_m = 2054 \pm 50 \text{ K}$ based on the study of Cezairiyand and McClure² since we have also adopted their measured heat capacity values. In addition there are many studies of binary phase diagrams which lend support to this adopted value.

Source	Zirconium Content (Wt%)	Transformation Hafnium Alloy	Temperature (K) Pure Hafnium
Dwez ³ unknown	1586 ± 10		
Fast (1952) ⁴	3	1960-2075	
Gibson <i>et al.</i> (1958) ⁵	0.01	2011	
Deardorff and Kato (1959) ⁶	1.2-8.8		2026 ± 20
Peterson and Beemsten (1960) ⁷	0.03	1966-2096	
Giessen <i>et al.</i> (1963) ⁸	2.3	1991 ± 15	2031 ± 20
Ross and Hume-Rothery (1963) ⁹	1.6	2236-2266 50	2271 ± 70
Krikorian and Wallace (1964) ¹⁰	0.02-3.45	2007-2100	2016 ± 14
Taylor and Doyle (1964) ¹¹	2.3	2226 ± 50	2270 ± 70
Romans <i>et al.</i> (1965) ¹²	1.5	2028	2053
Bates and Barnes (1967) ¹³	3.6	2033	
Peletskii and Druzhinin (1971) ¹⁴	0.66	1970 ± 5	
Carlson <i>et al.</i> (1973) ¹⁵	3.3	1990-2003	
Cezairiyand and McClure (1976) ²	3.12	2012 ± 10	2054

Cezairiyand and McClure² using a millisecond-resolution pulse-heating technique, measured the transformation enthalpy to be $33.1 \text{ J}\cdot\text{g}^{-1}$ ($1.412 \pm 0.05 \text{ kcal}\cdot\text{mol}^{-1}$). Peletskii and Druzhinin¹⁴ measured $29 \text{ J}\cdot\text{g}^{-1}$ ($1.237 \text{ kcal}\cdot\text{mol}^{-1}$), a value which is roughly 12% lower than that of Cezairiyand and McClure.² Marynyuk and Tsapkov,¹⁶ using a continuous-pulse heating technique, measured a transformation enthalpy of $1.24 \text{ kcal}\cdot\text{mol}^{-1}$. The samples used in all three studies contained significant amounts of zirconium wt %, ² 0.66 wt %, ¹⁴ and 0.7 wt %, ¹⁶ respectively. Hoerster *et al.*¹⁷ measured an enthalpy of transition of $0.52 \text{ kcal}\cdot\text{mol}^{-1}$ at 2090 K. We adopted $\Delta_{\alpha\beta} H^\circ = 1.412 \pm 0.05 \text{ kcal}\cdot\text{mol}^{-1}$ as derived from the study of Cezairiyand and McClure.²

Fusion Data

Refer to the liquid table.

Sublimation Data

The sublimation studies for β-Hf(cr) are summarized on the Hf(g) table. The enthalpy of sublimation for Hf(β,cr) is calculated as the difference in the enthalpies of formation at 298.15 K of Hf(g) and Hf(β,cr).

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Hafnium, Beta (β-Hf)

Hf₁(cr)

T/K	C _p J·K ⁻¹ ·mol ⁻¹	S ^o - [C _p - H ^o (T)]/T J·K ⁻¹ ·mol ⁻¹	H ^o - H ^o (T) kJ·mol ⁻¹	Δ _f H ^o kJ·mol ⁻¹	Standard State Pressure = p ^o = 0.1 MPa log K _r
0					
100					
200					
250					
298.15	17.747	61.104	61.104	0.	18.686
300	17.764	61.214	61.105	0.033	18.671
350	18.226	63.987	61.323	0.933	18.272
400	18.687	66.451	61.812	1.855	17.879
450	19.149	68.679	62.454	2.801	17.466
500	19.611	70.720	63.180	3.770	17.062
600	20.534	74.377	64.748	5.778	16.255
700	21.457	77.612	66.359	7.877	15.453
800	22.381	80.538	67.951	10.069	14.658
900	23.304	83.227	69.501	12.353	13.872
1000	24.227	85.750	71.000	14.730	13.095
1100	25.151	88.082	72.447	17.199	12.329
1200	26.074	90.310	73.844	19.760	11.573
1300	26.997	92.434	75.193	22.414	10.829
1400	27.921	94.468	76.497	25.160	10.104
1500	28.844	96.426	77.761	27.998	9.401
1600	29.767	98.317	78.987	30.928	8.720
1700	30.691	100.150	80.178	33.951	8.061
1800	31.614	101.930	81.338	37.067	7.424
1900	32.537	103.664	82.467	40.274	6.810
2000	33.461	105.356	83.569	43.574	6.218
2054.000	33.959	106.255	84.154	45.394	6.159
2100	34.384	107.011	84.646	46.966	6.100
2200	35.307	108.632	85.700	50.451	5.511
2300	36.231	110.222	86.732	54.028	4.922
2400	37.154	111.784	87.743	57.697	4.333
2500	38.077	113.353	88.736	61.542	3.744
2500.000	38.077	113.353	88.736	61.542	3.744
2600	39.001	114.965	89.712	65.396	3.155
2700	39.924	116.554	90.672	69.342	2.566
2800	40.847	117.922	91.615	73.381	1.977
2900	41.771	119.372	92.544	77.512	1.388
3000	42.694	120.704	93.459	81.735	0.799

PREVIOUS:

CURRENT March 1979

TK	C_p°	Enthalpy Reference Temperature = $T_r = 298.15$ K	$S^\circ - [C_p^\circ - H_f^\circ(T_r)]/T$	$H^\circ - H_f^\circ(T_r)$	ΔH_f°	Standard State Pressure = $p^\circ = 0.1$ MPa	$H_f(\text{Hf})$
	$\text{J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$	$\text{J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$	$\text{J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$	$\text{J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$	$\text{kJ}\cdot\text{mol}^{-1}$	log K _r	
0							
100							
200							
250							
298.15	17.747	71.938	71.938	0.	46.209	37.748	-6.613
300	17.764	72.048	71.939	0.033	46.194	37.695	-6.563
350	18.226	74.821	72.577	0.933	45.795	36.311	-5.419
400	18.687	77.285	74.646	1.855	44.563	34.983	-4.568
450	19.149	79.513	73.288	2.801	44.989	33.706	-3.912
500	19.611	81.554	74.014	3.770	44.585	32.474	-3.393
600	20.534	85.211	75.582	5.778	43.778	30.128	-2.623
700	21.457	88.446	77.193	7.677	42.976	27.916	-2.083
800	22.381	91.372	78.785	10.399	42.181	25.819	-1.686
900	23.304	94.061	80.335	12.533	41.395	23.821	-1.383
1000	24.227	96.564	81.834	14.730	40.619	21.910	-1.144
1100	25.151	98.916	83.281	17.199	39.852	20.076	-0.953
1200	26.074	101.144	84.678	19.760	39.097	18.312	-0.797
1300	26.997	103.268	86.027	22.414	38.353	16.610	-0.667
1400	27.921	105.302	87.231	25.160	37.627	14.965	-0.558
1500	28.844	107.260	88.595	27.998	36.924	13.371	-0.466
1600	29.767	109.151	89.821	30.928	36.243	11.823	-0.386
1700	30.691	110.984	91.012	33.951	35.584	10.317	-0.317
1800	31.614	112.764	92.172	37.067	34.948	8.849	-0.257
1820.000	31.799	113.114	92.400	37.701			
1820.000	37.656	113.114	92.400	37.701			
1900	37.656	114.734	93.306	40.713	34.773	7.406	-0.204
2000	37.656	116.666	94.426	44.479	34.646	5.969	-0.156
2100	37.656	118.503	95.529	48.244	28.802	4.669	-0.116
2200	37.656	120.255	96.614	52.010	29.083	3.513	-0.083
2300	37.656	121.929	97.678	55.776	29.271	2.346	-0.053
2400	37.656	123.531	98.722	59.541	29.368	1.173	-0.026
2500	37.656	125.068	99.746	63.307	29.288	0.	0.
2500.000	37.656	125.068	99.746	63.307			
2600	37.656	126.545	100.748	67.072	0.	0.	0.
2700	37.656	127.966	101.730	70.838	0.	0.	0.
2800	37.656	129.336	102.692	74.604	0.	0.	0.
2900	37.656	130.657	103.633	78.369	0.	0.	0.
3000	37.656	131.934	104.556	82.135	0.	0.	0.
3100	37.656	133.169	105.459	85.900	0.	0.	0.
3200	37.656	134.364	106.344	89.666	0.	0.	0.
3300	37.656	135.523	107.210	93.432	0.	0.	0.
3400	37.656	136.647	108.060	97.197	0.	0.	0.
3500	37.656	137.739	108.892	100.963	0.	0.	0.
3600	37.656	138.799	109.708	104.728	0.	0.	0.
3700	37.656	139.831	110.508	108.494	0.	0.	0.
3800	37.656	140.835	111.293	112.260	0.	0.	0.
3900	37.656	141.814	112.063	116.025	0.	0.	0.
4000	37.656	142.767	112.819	119.791	0.	0.	0.
4100	37.656	143.697	113.561	123.556	0.	0.	0.
4200	37.656	144.604	114.289	127.322	0.	0.	0.
4300	37.656	145.490	115.005	131.088	0.	0.	0.
4400	37.656	146.356	115.707	134.853	0.	0.	0.
4500	37.656	147.202	116.398	138.619	0.	0.	0.
4600	37.656	148.030	117.077	142.384	0.	0.	0.
4700	37.656	148.840	117.744	146.150	0.	0.	0.
4800	37.656	149.632	118.400	149.916	0.	0.	0.
4900	37.656	150.409	119.045	153.681	0.	0.	0.
4963.793	37.656	150.896	119.452	156.083			
5000	37.656	151.170	119.680	157.447	-560.219	4.086	-0.043
5100	37.656	151.915	120.305	161.212	-560.290	15.373	-0.157
5200	37.656	152.646	120.920	164.978	-560.407	26.662	-0.268
5300	37.656	153.364	121.525	168.744	-560.568	37.953	-0.374
5400	37.656	154.068	122.121	172.509	-560.776	49.248	-0.476
5500	37.656	154.759	122.709	176.275	-561.030	60.547	-0.575

PREVIOUS:

CURRENT: March 1979

Hafnium (Hf) $H_f(\text{Hf})$

$S^\circ(298.15\text{ K}) = [71.938]\text{ J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$
 $T_{\text{fus}} = 2500 \pm 20\text{ K}$
 $\Delta_f H^\circ(298.15\text{ K}) = [46.209]\text{ kJ}\cdot\text{mol}^{-1}$
 $\Delta_{\text{vap}} H^\circ = [29.288 \pm 4.2]\text{ kJ}\cdot\text{mol}^{-1}$

Enthalpy of Formation

The enthalpy of formation is calculated from that of the β -crystal by addition of $\Delta_{\text{vap}} H^\circ$ and the difference in enthalpy, $H^\circ(2500\text{ K}) - H^\circ(298.15\text{ K})$, between the β -crystal and liquid.

Heat Capacity and Entropy

There are no heat capacity or enthalpy studies covering the liquid region of hafnium. A constant value of $C_p^\circ = 9.0\text{ cal}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$ is assumed for the region 1820–5500 K. A glass transition is assumed at 1820 K below which extrapolated β -Hf heat capacity values are used. The entropy is calculated in a manner similar to that used for the enthalpy of formation.

Fusion Data

Garg and Ackermann,¹ using pyrometric techniques, measured the melting point of hafnium as $2501 \pm 3\text{ K}$. Hultgren *et al.*,² reviewed nine studies available through 1955 and recommended $T_{\text{fus}} = 2500 \pm 20\text{ K}$. We adopted $T_{\text{fus}} = 2500 \pm 20\text{ K}$.

The studies (and the reported melting temperatures in K) examined by Hultgren *et al.*,² are: DeBoer and Fast,³ 2503 ± 50 ; Skinner *et al.*,⁴ 2498; Litton,⁵ 2403; Adenstedt,⁶ 2248; Spedding,⁷ 2508 ± 5 ; Deardoff and Hayes,⁸ (2495 \pm 20; Gregorovich,⁹ 2116; Taylor *et al.*,¹⁰ 2503 \pm 20.

Ackermann and Rauh¹¹ measured a melting point of $2467 \pm 4\text{ K}$ in a HfO₂ container. However, they state that the melting point may be as high as 2495 K since their sample contained 0.7 wt % Zr.

The enthalpy melting for Hf has not been measured. Various estimates and calculations have been made. Martynyuk *et al.*¹² correlated graphically $\Delta_{\text{vap}} H^\circ$ versus T_{fus} for many metals and used the resulting linear relationship to estimate $\Delta_{\text{vap}} H^\circ = 7.0\text{ kcal}\cdot\text{mol}^{-1}$. We adopt this value. Ackermann and Rauh¹³ measured vapor pressures over Hf(β ,cr) and Hf(l), adjusted the vapor pressures for Hf(β ,cr) to match those of Hf(l) at T_{fus} , and derived $\Delta_{\text{vap}} H^\circ = 6.2\text{ kcal}\cdot\text{mol}^{-1}$.

Vaporization Data

The vaporization studies are summarized on the ideal gas table.

The boiling point is calculated as that temperature for which $\Delta G^\circ = 0$ for Hf(l) = Hf(g). $\Delta_{\text{vap}} H^\circ$ is the corresponding enthalpy change. T_{bp} is the temperature at which the fugacity is one bar. The normal boiling point ($p = 1$ bar) would be a slightly lower temperature.

References

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Hafnium (Hf)

A₁ = 178.49 Hafnium (Hf)

CRYSTAL(α-β)-LIQUID

0 to 2054 K crystal, alpha
2054 to 2500 K crystal, beta
above 2500 K liquid

Refer to the individual tables for details.

Hf (cr,l)

T/K	Enthalpy Reference Temperature = T _r = 298.15 K		Standard State Pressure = p° = 0.1 MPa		log K _r
	C _p ^o	S° - [C _p ^o - H ^o (T _r)]/T	H° - H ^o (T _r)	Δ _r H ^o	
0	0	INFINITE	0	0	0
100	20.580	17.753	-5.842	0	0
200	24.418	33.561	-4.764	0	0
250	25.110	39.086	-2.952	0	0
298.15	25.687	43.560	0	0	0
300	25.708	43.719	0.048	0	0
350	26.247	47.723	1.347	0	0
400	26.751	51.261	2.672	0	0
450	27.230	54.439	4.021	0	0
500	27.692	57.332	5.394	0	0
600	28.583	62.460	8.208	0	0
700	29.445	66.932	11.110	0	0
800	30.288	70.919	14.097	0	0
900	31.120	74.534	17.167	0	0
1000	31.943	77.856	20.370	0	0
1100	32.759	80.938	23.556	0	0
1200	33.572	83.824	26.872	0	0
1300	34.384	86.543	30.270	0	0
1400	35.194	89.113	33.741	0	0
1500	35.765	91.538	37.283	0	0
1600	36.466	93.889	40.894	0	0
1700	37.167	96.121	44.576	0	0
1800	37.868	98.265	48.328	0	0
1900	38.569	100.331	52.149	0	0
2000	39.269	102.327	56.041	0	0
2054.000	39.648	103.378	58.172	0	0
2054.000	33.959	106.255	64.080	ALPHA <- -> BETA TRANSITION	0
2100	34.384	107.011	65.652	0	0
2200	35.307	108.632	69.136	0	0
2300	36.231	110.222	72.713	0	0
2400	37.154	111.784	76.383	0	0
2500	38.077	113.353	80.228	0	0
2500.000	38.077	113.353	80.228	BETA <- -> LIQUID TRANSITION	0
2500.000	37.856	125.068	109.516	0	0
2600	37.656	126.545	113.281	0	0
2700	37.656	127.966	117.047	0	0
2800	37.656	129.336	120.813	0	0
2900	37.656	130.657	124.578	0	0
3000	37.656	131.934	128.344	0	0
3100	37.656	133.169	132.109	0	0
3200	37.656	134.364	135.875	0	0
3300	37.656	135.523	139.641	0	0
3400	37.656	136.647	143.406	0	0
3500	37.656	137.739	147.172	0	0
3600	37.656	138.799	150.937	0	0
3700	37.656	139.831	154.703	0	0
3800	37.656	140.835	158.469	0	0
3900	37.656	141.814	162.234	0	0
4000	37.656	142.767	166.000	0	0
4100	37.656	143.697	169.765	0	0
4200	37.656	144.604	173.531	0	0
4300	37.656	145.490	177.297	0	0
4400	37.656	146.356	181.062	0	0
4500	37.656	147.202	184.828	0	0
4600	37.656	148.030	188.593	0	0
4700	37.656	148.840	192.359	0	0
4800	37.656	149.632	196.125	0	0
4900	37.656	150.409	199.890	0	0
4963.793	37.656	150.896	202.292	FUGACITY = 1 bar	0
5000	37.656	151.170	203.656	---	-560.219
5100	37.656	151.915	207.421	---	4.086
5200	37.656	152.646	211.187	---	-0.437
5300	37.656	153.364	214.953	---	15.373
5400	37.656	154.068	218.718	---	26.662
5500	37.656	154.759	222.484	---	37.953
				---	49.248
				---	60.547
				---	-0.575

PREVIOUS.

CURRENT: March 1979

Hafnium (Hf)

Hf_l(cr,l)

Hafnium (Hf)

IP(Hf, g) = 54700 ± 600 cm⁻¹
S^o(298.15 K) = 186.897 ± 0.2 J·K⁻¹·mol⁻¹

IDEAL GAS

A₁ = 178.49

ΔH^o(0 K) = 618.0 ± 6.3 kJ·mol⁻¹
ΔH^o = (298.15 K) = 618.4 ± 6.3 kJ·mol⁻¹

Electronic Levels and Quantum Weights	g _i
State	
3F ₂	0.00
3F ₃	2356.68
3F ₄	4567.64
IP	53853.61
	54700

Enthalpy of Formation

There are six sublimation studies and two vaporization studies from which an enthalpy of formation for Hf(g) could be derived. A plot of these vapor pressure data, log p vs 1/T, reveals considerable discrepancy between the various studies. In the liquid region, the vapor pressure values of Koch *et al.*¹ and Ackermann and Rauh² are in close agreement. The pressures of the former study are 5% higher at 2500 K but become 10% lower at 2800 K. The measured temperatures in the former study¹ were adjusted (i.e., the pyrometer reading) by Koch *et al.* so that at the observed melting point the temperature would be 2500 K. The sample purity was not stated. In the latter study² the reported vapor pressures were corrected pressures (assuming ideal solution) from a eutectic of Hf and W. The Hf sample had a measured melting point of 2464 K; the purity was not reported.

The sublimation studies of Golubov and Mikul'skaya³ and Ackermann and Rauh² spanned a temperature range which involved the α- and β-phases of hafnium, yet neither study mentioned the characterization of the condensed phase. The study of Golubov and Mikul'skaya³ is not considered further since their reported vapor pressure equation is ambiguous and cannot be easily modified to yield reasonable vapor pressures. In general terms, the sublimation pressures of Ackermann and Rauh,² Kibler *et al.*⁴, and McClaine and Blackburn⁵ are in reasonable agreement. The pressures of Panish and Reif⁶ are 60% above these three studies,^{2,4,5} there is considerable scatter with one distinctly low pressure point at 2113 K. On the other hand, the results of Trulsson *et al.*⁷ are substantially lower by 50% than the three studies^{2,4,5} with two distinctly lower points.

A 2nd and 3rd law analysis is given in the following table. We adopt ΔH^of(Hf, g, 298.15 K) = 147.8 ± 1.5 kcal·mol⁻¹. This result is based on the reasonable consistency of the two vapor pressure studies^{2,4} with each other and with our adopted thermodynamic functions as evidenced by the small values of the drift. Hultgren *et al.*,⁸ using different thermodynamic functions and data available through 1966, recommended an enthalpy of formation of 148.0 ± 1.0 kcal·mol⁻¹ based heavily on the study by Kibler *et al.*⁴ Other values for ΔH^of(298.15 K), also derived from vapor pressure studies, have been reported by Krupka,⁹ Krikorian,¹⁰ and Kibler *et al.*¹¹

Source (Year)	Reaction* Pts	T/K	Method	ΔH ^o f(298.15 K), kcal·mol ⁻¹	Dnft, cal·K ⁻¹ ·mol ⁻¹	ΔH ^o f(298.15 K), kcal·mol ⁻¹
Kibler <i>et al.</i> (1963) ¹¹	A 8	2035-2325	Langmuir	141.5 ± 2.4	143.4 ± 0.5	0.9 ± 1.1
Panish and Reif (1963) ⁶	A 6	2066-2274	Langmuir	160.3 ± 15.5	140.9 ± 2.7	-9.0 ± 7.2
McClaine (1964) ⁵	A 5	2200-2363	Langmuir	124.3 ± 5.7	144.5 ± 1.3	8.8 ± 2.5
Trulsson <i>et al.</i> (1965) ⁷	A 15 ^b	2075-2273	Knudsen	145.1 ± 4.2	145.9 ± 0.7	0.4 ± 1.9
Ackermann and Rauh (1972) ²	A eqn	1950-2464	mass eff.	145.4	143.6	-0.8
Koch <i>et al.</i> (1968) ¹	B 17	2500-2810	Langmuir	131.6 ± 3.4	136.9 ± 1.2	2.0 ± 1.3
Ackermann and Rauh (1972) ²	B eqn	1464-2800	mass eff.	140.1	136.7	-1.3

*Reaction. A) Hf(β,cr) = Hf(g) B) Hf(α) = Hf(g)
^bTwo points discarded due to a statistical test.

Heat Capacity and Entropy

The electronic energy levels are given in the compilation by Meggers and Moore.¹² Although we have listed only the ground state, the lowest two excited states, the highest observed excited state (below the ionization potential), and the ionization potential for Hf(g), all levels listed by Meggers and Moore,¹² as well as estimated levels (for n = 5,6,7), are used in the calculation. The 233 observed levels, two of which lie above the ionization potential, are too numerous to list completely. In our calculations, the missing levels for n = 6 and 7 have been arbitrarily added near the ionization limit. The calculations indicate that for Hf(g) the thermodynamic functions up to at least 3000 K are independent of the estimated missing levels (for n = 6 and 7), the cut-off procedure, and the inclusion of n = 7 levels. At this temperature there are no experimental heat capacity enthalpy, or vapor pressure data. The Gibbs energy function is essentially unaffected up to 5500 K.

References

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Hafnium (Hf)

Hf(g)

T/K	C _p ^o	S ^o - (G ^o - HF(T))/T	H ^o - HF(T)	ΔH ^o f	Standard State Pressure = P ^o = 0.1 MPa	log K _r	Hf(g)
0	0	0	INFINITE	0	618.040	INFINITE	
100	20.786	164.188	205.380	-6.198	618.040		
200	20.786	178.596	188.759	-4.119	619.040		
298.15	20.789	183.235	187.240	-2.041	618.816		
300	20.803	186.897	186.897	-1.001	618.617		
350	20.804	187.026	186.898	0	618.395		
380	20.854	190.235	187.151	0.038	618.386		
400	20.960	193.027	187.445	1.080	618.128		
450	21.140	195.505	188.145	2.125	617.848		
500	21.397	197.745	189.265	3.177	617.551		
600	22.113	201.706	192.707	4.240	617.241		
700	23.012	205.181	192.977	6.414	616.600		
800	23.997	208.317	194.544	8.669	615.954		
900	24.978	211.200	196.236	11.019	615.317		
1000	25.925	213.881	197.868	13.467	614.695		
1100	26.806	216.394	199.439	16.013	614.088		
1200	27.603	218.761	200.952	18.650	613.494		
1300	28.305	220.999	202.409	21.371	612.894		
1400	28.912	223.119	203.813	24.167	612.293		
1500	29.424	225.132	205.168	27.029	611.683		
1600	29.847	227.045	206.476	29.947	611.059		
1700	30.190	228.865	207.740	32.911	610.412		
1800	30.465	230.599	208.962	35.913	609.733		
1900	30.681	232.252	210.144	38.947	609.014		
2000	30.832	233.830	211.290	42.004	608.250		
2100	30.986	235.339	212.399	45.081	607.435		
2200	31.095	236.783	213.475	48.174	606.917		
2300	31.187	238.167	214.519	51.278	606.537		
2400	31.270	239.498	215.532	54.372	606.074		
2500	31.351	240.775	216.516	57.451	605.528		
2600	31.456	242.006	217.473	60.546	605.000		
2700	31.528	243.194	218.404	63.646	604.899		
2800	31.652	244.342	219.310	66.733	604.822		
2900	31.750	245.454	220.192	70.091	604.656		
3000	31.884	246.533	221.052	73.660	604.597		
3100	32.037	247.581	221.891	77.442	604.593		
3200	32.208	248.601	222.710	81.338	604.524		
3300	32.399	249.595	223.510	85.350	604.524		
3400	32.610	250.565	224.291	89.380	604.524		
3500	32.841	251.513	225.056	92.603	604.524		
3600	33.090	252.442	225.803	95.899	604.524		
3700	33.359	253.352	226.536	99.271	604.524		
3800	33.645	254.246	227.253	102.721	604.524		
3900	33.948	255.124	227.957	105.951	604.524		
4000	34.267	255.987	228.647	109.362	604.524		
4100	34.602	256.837	229.324	112.805	604.524		
4200	34.951	257.675	229.989	116.282	604.524		
4300	35.313	258.502	230.642	119.792	604.524		
4400	35.688	259.318	231.285	123.345	604.524		
4500	36.074	260.124	231.917	126.933	604.524		
4600	36.471	260.921	232.539	130.561	604.524		
4700	36.878	261.710	233.151	134.228	604.524		
4800	37.294	262.494	233.754	137.936	604.524		
4900	37.720	263.264	234.348	141.687	604.524		
4963.793	37.996	263.754	234.723	144.102	604.524		
5000	38.154	264.031	234.934	145.481	0	0	
5100	38.595	264.790	235.512	149.518	0	0	
5200	39.044	265.544	236.083	153.200	0	0	
5300	39.501	266.292	236.646	157.127	0	0	
5400	39.964	267.035	237.202	161.100	0	0	
5500	40.434	267.773	237.751	165.120	0	0	
5600	40.910	268.505	238.293	169.187	0	0	
5700	41.392	269.234	238.830	173.302	0	0	
5800	41.879	269.958	239.360	177.465	0	0	
5900	42.372	270.678	239.885	181.678	0	0	
6000	42.870	271.394	240.404	185.940	0	0	

PREVIOUS March 1979 (1 atm) CURRENT March 1979 (1 bar)

Hafnium, Ion (Hf⁺) M_r = 178.48945 Hafnium, Ion (Hf⁺) Hf(g)

$\Delta H_f^\circ(0\text{ K}) = 1272.4 \pm 4.0\text{ kJ}\cdot\text{mol}^{-1}$
 $\Delta H_f^\circ(298.15\text{ K}) = [1278.950]\text{ kJ}\cdot\text{mol}^{-1}$

T/K	Enthalpy Reference Temperature = T _r = 298.15 K		Standard State Pressure = p ^o = 0.1 MPa		log K _r
	C _p ^o	S ^o - [G ^o - H ^o (T)]/T	H ^o - H ^o (T)	ΔG ^o	
		J·K ⁻¹ ·mol ⁻¹	J·K ⁻¹ ·mol ⁻¹	kJ·mol ⁻¹	
0	0	INFINITE	-6.197	1272.397	
100	20.786	162.333	-4.119		-215.581
200	20.786	176.741	-2.640		-214.199
250	20.786	181.379	-1.001		-182.377
298.15	20.786	185.040	0		-158.496
300	20.786	185.169	0.038	1278.950	-139.911
350	20.786	188.373	1.078		-125.035
400	20.786	191.149	2.117		-102.701
450	20.786	193.597	3.156		-75.478
500	20.786	195.787	4.196		-51.946
600	20.786	199.577	6.274		-28.680
700	20.786	202.781	8.353		-27.991
800	20.786	205.556	10.431		-26.015
900	20.786	208.005	12.510		-24.237
1000	20.786	210.195	14.589		-22.631
1100	20.787	212.176	16.667		-21.174
1200	20.789	213.985	18.746		-19.843
1300	20.794	215.649	20.825		-18.622
1400	20.804	217.190	22.903		-17.499
1500	20.823	218.626	24.986		-16.485
1600	20.857	219.971	27.070		-15.545
1700	20.910	221.237	29.158		-14.672
1800	20.991	222.434	31.253		-13.859
1900	21.107	223.572	33.358		-13.099
2000	21.264	224.658	35.476		-12.388
2100	21.472	225.701	37.612		-11.721
2200	21.737	226.705	39.772		-11.094
2300	22.065	227.679	41.963		-10.503
2400	22.462	228.626	44.187		-9.945
2500	22.931	229.552	46.456		-9.418
2600	23.477	230.462	48.776		-8.918
2700	24.100	231.359	51.154		-8.444
2800	24.800	232.248	53.599		-7.994
2900	25.576	233.132	56.117		-7.566
3000	26.424	234.013	58.716		-7.158
3100	27.341	234.894	61.404		-6.768
3200	28.320	235.778	64.187		-6.396
3300	29.355	236.665	67.070		-6.041
3400	30.437	237.557	70.059		-5.700
3500	31.559	238.455	73.159		-5.374
3600	32.711	239.360	76.372		-5.061
3700	33.883	240.273	79.702		-4.760
3800	35.066	241.192	83.149		-4.471
3900	36.249	242.118	86.715		-4.199
4000	37.434	243.051	90.399		-3.941
4100	38.580	243.989	94.199		-3.696
4200	39.710	244.932	98.114		-3.464
4300	40.805	245.880	102.140		-3.242
4400	41.857	246.830	106.277		-3.030
4500	42.862	247.782	110.510		-2.826
4600	43.812	248.734	114.844		-2.630
4700	44.704	249.686	119.270		-2.441
4800	45.534	250.636	123.783		-2.258
4900	46.299	251.583	128.375		-2.081
5000	46.999	252.526	133.040		-1.910
5100	47.631	253.463	137.772		-1.754
5200	48.197	254.393	142.564		-1.603
5300	48.696	255.316	147.409		-1.457
5400	49.130	256.231	152.307		-1.315
5500	49.501	257.136	157.253		-1.177
5600	49.811	258.030	162.246		-1.042
5700	50.063	258.914	167.282		-0.911
5800	50.260	259.787	172.356		-0.783
5900	50.405	260.647	177.444		-0.658
6000	50.502	261.495	182.290		-0.536

PREVIOUS: March 1979 (1 atm)

CURRENT: March 1984 (1 bar)

IP(Hf⁺, g, 0 K) = 120000 ± 10000 cm⁻¹
S^o(298.15 K) = 185.040 ± 0.01 J·K⁻¹·mol⁻¹

Electronic Levels and Quantum Weights	g _r
State	
² D _{3/2}	4
² D _{5/2}	6
.	.
.	.
.	.
IP	10
	120000

Enthalpy of Formation
ΔH^o(Hf⁺, g, 0 K) is calculated from ΔH^o(Hf, g, 0 K) using the spectroscopic value of IP(Hf) = 54700 ± 600 cm⁻¹ (654.358 ± 1.18 kJ·mol⁻¹) from Meggers and Moore.² The ionization limit is converted from cm⁻¹ to kJ·mol⁻¹ using the factor, 1 cm⁻¹ = 0.01196266 kJ·mol⁻¹, which is derived from the 1973 CODATA fundamental constants.³ Rosenstock *et al.*⁴ and Levin and Lias⁵ have summarized additional ionization and appearance potential data.

ΔH^o(Hf⁺, g, 298.15 K) is calculated from ΔH^o(Hf, g, 0 K) by using IP (Hf) with JANAF⁶ enthalpies, H^o(0 K) - H^o(298.15 K), for Hf(g), Hf⁺(g), and e⁻(g). ΔH^o(Hf → Hf⁺ + e⁻, 298.15 K) differs from a room temperature threshold energy due to inclusion of these enthalpies and to threshold effects discussed by Rosenstock *et al.*⁴ ΔH^o(298.15 K) should be changed by -6.197 kJ·mol⁻¹ if it is to be used in the ion convention that excludes the enthalpy of the electron.

Heat Capacity and Entropy
The electronic energy levels are given in the compilation by Moore.⁶ Although we have listed only the ground state, the first excited state, the highest observed excited state, and the ionization potential for Hf⁺(g), all levels listed by Moore,⁶ as well as estimated levels (for n = 6 and 7), are used in the calculation. The 121 observed levels are too numerous to list completely. In our calculations the missing levels for n = 6 and 7 have been arbitrarily added near the ionization limit. The calculations indicate that for Hf⁺(g) the thermodynamic functions up to 5000 K are independent of the estimated missing levels (for n = 6 and 7), the cut-off procedure, and the inclusion of n = 7 levels. The free energy function is unaffected up to 10000 K. The reported uncertainty in S^o is due to uncertainties in the gram formula weight and the fundamental constants. Extension of these calculations above 6000 K may require consideration of the higher excited states (n > 7), more precise estimation of the missing levels (for all n), and utilization of proper fill and cut-off procedures.⁷

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Hafnium, Ion (Hf⁺)

IDEAL GAS

Hafnium, Ion (Hf⁺)

EA(Hf, g) = 0.0 eV
 S⁰(298.15 K) = 185.040 ± 0.002 J·K⁻¹·mol⁻¹

Electronic Level and Quantum State	Weight g _i
¹ F _{3/2}	4

Enthalpy of Formation

ΔH⁰(Hf⁺, g, 0 K) is calculated from ΔH⁰(Hf, g, 0 K) using the adopted electron affinity of EA(Hf) = -0.0 eV. This value, recommended by Hotop and Lineberger,³ is based on a semiempirical extrapolation.^{3,4} Additional information on Hf⁺(g) and may be obtained in the critical discussions of Hotop and Lineberger,^{2,4} Rosenstock *et al.*,⁵ and Massey.⁶
 ΔH⁰(Hf⁺, g, 298.15 K) is obtained from ΔH⁰(Hf, g, 0 K) by using EA(Hf) with JANAF¹ enthalpies, H⁰(0 K)-H⁰(298.15 K), for Hf⁰(g), Hf(g), and e⁻(ref). ΔH⁰(Hf⁺ → Hf + e⁻, 298.15 K) differs from a room-temperature threshold energy due to inclusion of these enthalpies and to threshold effects discussed by Rosenstock *et al.*,⁵ Δ₁H⁰(298.15 K) should be changed by +6.197 kJ·mol⁻¹ if it is to be used in the ion convention that excludes the enthalpy of the electron.

Heat Capacity and Entropy

The ground state electronic configuration for Hf⁺(g) is given by Hotop and Lineberger^{2,4} and Rosenstock *et al.*,⁵ Lacking any experimental evidence as to the stability of any excited states, we assume that no stable excited states exist.

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Hafnium, Ion (Hf⁺)

M_r = 178.49055

Δ₁H⁰(0 K) = 618.040 ± 6.3 kJ·mol⁻¹
 Δ₁H⁰(298.15 K) = [612.197] kJ·mol⁻¹

T/K	C _p ^o	Enthalpy Reference Temperature = T _r = 298.15 K		Standard State Pressure = p ^o = 0.1 MPa		log K _r
		S ^o - [G ^o - H ^o (T _r)]/T	H ^o - H ^o (T _r)]/T	Δ ₁ H ^o	Δ ₁ G ^o	
0	0	INFINITE	0	618.040		
100	20.786	162.333	-6.197		576.270	-100.960
200	20.786	166.741	-4.119		576.047	-100.299
250	20.786	181.579	-2.040		570.132	-85.088
298.15	20.786	185.040	-1.001		564.405	-71.704
300	20.786	185.041	0		558.846	-64.869
350	20.786	188.373	0.038		553.438	-57.817
400	20.786	191.149	0.078		603.989	-47.275
450	20.786	193.597	0.116		533.098	-39.780
500	20.786	195.787	0.156		598.101	-34.187
600	20.786	199.577	0.274		514.455	-29.858
700	20.786	202.781	0.433		505.671	-26.414
800	20.786	205.556	0.610		588.642	-23.610
900	20.786	208.005	0.810		489.040	-21.287
1000	20.786	210.195	1.030		581.325	-19.333
1100	20.786	212.176	1.270		585.928	-19.333
1200	20.786	213.984	1.530		581.928	-19.333
1300	20.786	215.648	1.810		578.456	-17.668
1400	20.786	217.189	2.110		473.531	-16.233
1500	20.786	218.623	2.430		466.159	-14.986
1600	20.786	219.964	2.780		571.303	-14.986
1700	20.786	221.224	3.150		561.621	-13.892
1800	20.786	222.422	3.540		563.870	-12.926
1900	20.786	223.556	3.950		560.048	-12.068
2000	20.786	224.622	4.380		556.156	-11.301
2100	20.786	225.617	4.830		546.546	-10.615
2200	20.786	226.534	5.300		543.061	-9.999
2300	20.786	227.350	5.790		539.484	-9.440
2400	20.786	228.092	6.300		535.815	-8.931
2500	20.786	228.741	6.830		531.970	-8.466
2600	20.786	229.306	7.380		498.916	-8.064
2700	20.786	230.840	7.950		493.150	-7.694
2800	20.786	231.596	8.540		493.385	-7.354
2900	20.786	232.326	9.150		487.619	-7.038
3000	20.786	233.030	9.780		483.854	-6.746
3100	20.786	233.712	10.430		480.088	-6.476
3200	20.786	234.372	11.100		476.322	-6.224
3300	20.786	235.012	11.790		472.557	-5.989
3400	20.786	235.632	12.500		468.791	-5.770
3500	20.786	236.235	13.230		465.026	-5.565
3600	20.786	236.820	14.000		461.260	-5.373
3700	20.786	237.390	14.800		457.494	-5.193
3800	20.786	237.944	15.630		453.729	-5.024
3900	20.786	238.484	16.490		449.963	-4.864
4000	20.786	239.010	17.380		446.198	-4.714
4100	20.786	239.524	18.300		442.432	-4.573
4200	20.786	240.024	19.250		438.666	-4.439
4300	20.786	240.514	20.230		434.901	-4.313
4400	20.786	240.991	21.240		431.135	-4.193
4500	20.786	241.459	22.280		427.370	-4.080
4600	20.786	241.915	23.350		423.604	-3.973
4700	20.786	242.362	24.450		419.838	-3.871
4800	20.786	242.800	25.580		416.073	-3.774
4900	20.786	243.229	26.740		412.307	-3.682
5000	20.786	243.649	27.930		408.541	-3.597
5100	20.786	244.060	29.150		358.202	-3.669
5200	20.786	244.464	30.410		358.313	-3.700
5300	20.786	244.860	31.710		378.499	-3.730
5400	20.786	245.248	33.050		388.759	-3.760
5500	20.786	245.630	34.430		399.093	-3.790
5600	20.786	246.004	35.850		409.501	-3.820
5700	20.786	246.372	37.310		419.989	-3.849
5800	20.786	246.734	38.810		430.555	-3.877
5900	20.786	247.089	40.340		441.161	-3.906
6000	20.786	247.438	41.900		451.858	-3.934

PREVIOUS: March 1979 (1 atm)

CURRENT: March 1984 (1 bar)

Hafnium, Ion (Hf⁺)

Hf⁺(g)

Hafnium

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Continuation of discussions of selected Hf species

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Mercury (Hg)

$A_r = 200.59$ Mercury (Hg)

REFERENCE STATE

0 to 234.29 K crystal
 234.29 to 629.839 K liquid
 above 629.839 K ideal monatomic gas

Refer to the individual tables for details.

Hg₁(ref)

T/K	C _p ^o	S ^o - [G ^o - H ^o (T)]/T	Enthalpy Reference Temperature = T _r = 298.15 K J·K ⁻¹ ·mol ⁻¹	Standard State Pressure = P ^o = 0.1 MPa kJ·mol ⁻¹		
				H ^o - H ^o (T _r)	ΔH ^o	ΔG ^o
				log K _r		
0	0	INFINITE	0	-9.343	0	0
100	24.255	37.219	113.592	-7.637	0	0
200	27.275	55.022	80.284	-5.052	0	0
234.290	28.485	59.428	76.915	-4.097	CRYSTAL → LIQUID	
234.290	28.476	69.225	76.915	-1.802	TRANSITION	
298.15	27.978	76.028	76.028	0	0	0
300	27.963	76.201	76.028	0.052	0	0
400	27.414	84.161	77.118	2.817	0	0
500	27.175	90.248	79.158	5.545	0	0
600	27.139	95.197	81.432	8.259	0	0
629.839	27.164	96.514	82.115	9.069	LIQUID → IDEAL GAS	
629.839	20.786	190.515	82.115	68.274	FUGACITY = 1 bar	
700	20.786	192.710	93.092	69.733	0	0
800	20.786	195.486	105.722	71.811	0	0
900	20.786	197.934	115.834	73.890	0	0
1000	20.786	200.124	124.156	75.969	0	0
1100	20.786	202.105	131.153	78.047	0	0
1200	20.786	203.914	137.143	80.126	0	0
1300	20.786	205.578	142.344	82.204	0	0
1400	20.786	207.118	146.916	84.283	0	0
1500	20.786	208.552	150.978	86.362	0	0
1600	20.786	209.894	154.619	88.440	0	0
1700	20.786	211.154	157.908	90.519	0	0
1800	20.786	212.342	160.899	92.597	0	0
1900	20.786	213.466	163.636	94.676	0	0
2000	20.786	214.532	166.155	96.755	0	0
2100	20.786	215.546	168.483	98.833	0	0
2200	20.786	216.513	170.644	100.912	0	0
2300	20.786	217.437	172.659	102.990	0	0
2400	20.786	218.322	174.543	105.069	0	0
2500	20.786	219.170	176.311	107.148	0	0
2600	20.786	219.986	177.975	109.226	0	0
2700	20.786	220.770	179.546	111.305	0	0
2800	20.786	221.526	181.032	113.383	0	0
2900	20.786	222.253	182.441	115.462	0	0
3000	20.786	222.960	183.780	117.541	0	0
3100	20.786	223.642	185.055	119.619	0	0
3200	20.786	224.302	186.271	121.698	0	0
3300	20.787	224.941	187.433	123.776	0	0
3400	20.787	225.562	188.546	125.855	0	0
3500	20.787	226.164	189.612	127.934	0	0
3600	20.788	226.750	190.635	130.013	0	0
3700	20.789	227.319	191.619	132.091	0	0
3800	20.790	227.874	192.566	134.170	0	0
3900	20.791	228.414	193.478	136.249	0	0
4000	20.793	228.940	194.358	138.329	0	0
4100	20.795	229.454	195.208	140.408	0	0
4200	20.798	229.955	196.029	142.488	0	0
4300	20.802	230.444	196.824	144.568	0	0
4400	20.807	230.923	197.594	146.648	0	0
4500	20.813	231.390	198.339	148.729	0	0
4600	20.820	231.848	199.063	150.811	0	0
4700	20.829	232.296	199.765	152.893	0	0
4800	20.839	232.734	200.448	154.977	0	0
4900	20.851	233.164	201.111	157.061	0	0
5000	20.866	233.586	201.756	159.147	0	0
5100	20.882	233.999	202.384	161.234	0	0
5200	20.902	234.403	202.996	163.324	0	0
5300	20.924	234.803	203.593	165.413	0	0
5400	20.949	235.194	204.174	167.508	0	0
5500	20.978	235.579	204.742	169.603	0	0
5600	21.010	235.957	205.296	171.704	0	0
5700	21.046	236.329	205.837	173.807	0	0
5800	21.087	236.696	206.366	175.913	0	0
5900	21.132	237.057	206.883	178.024	0	0
6000	21.182	237.412	207.389	180.140	0	0

PREVIOUS: December 1961 (1 atm) CURRENT: December 1961 (1 bar)

Mercury (Hg)

Hg₁(ref)